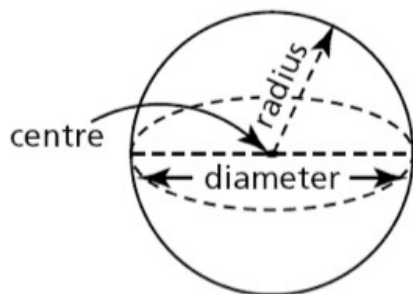


# Spheres

**Sphere** = the set of points that are the same distance away from a fixed point, which is the centre.

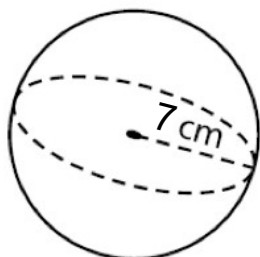


$$SA = 4\pi r^2$$

$$V = \frac{4}{3}\pi r^3$$

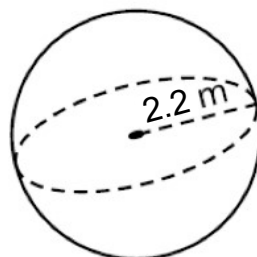
**Ex. 1** Find the surface area of each sphere:

a)



$$SA = 4\pi(7)^2$$
$$= 615.75 \text{ cm}^2$$

b)



$$SA = 4\pi(2.2)^2$$
$$= 60.82 \text{ m}^2$$

**Ex 2.**

The diameter of a softball is approximately 4 in. Determine the surface area of a softball to the nearest square inch.

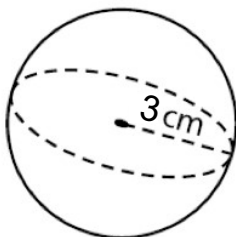
$$r = 2 \text{ in}$$

$$SA = 4\pi(2)^2$$
$$= 50.27 \text{ in}^2$$



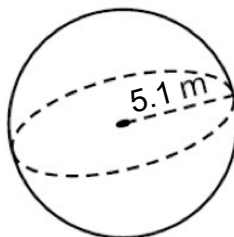
**Ex 3.** Find the volume of each sphere:

a)



$$V = \frac{4\pi(3)^3}{3}$$
$$= 113.10 \text{ cm}^3$$

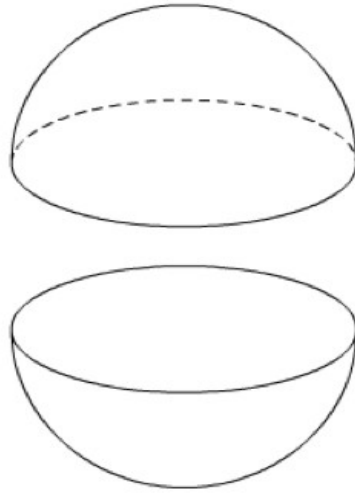
b)



$$V = \frac{4\pi(5.1)^3}{3}$$
$$= 555.65 \text{ m}^3$$

# Hemispheres

When a sphere is cut in half, two *hemispheres* are formed.



hemispheres

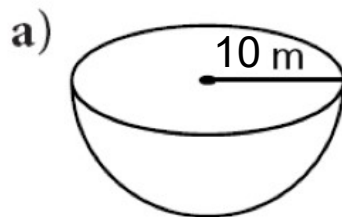
**SA** = half a sphere + area of a circle

$$\begin{aligned} &= \frac{4\pi r^2}{2} + \pi r^2 \\ &= 2\pi r^2 + \pi r^2 \\ &= 3\pi r^2 \end{aligned}$$

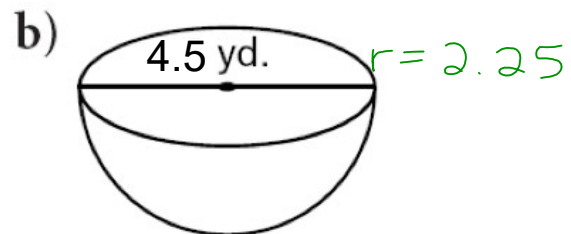
**V** = half a sphere

$$\begin{aligned} V &= \left(\frac{1}{2}\right)\left(\frac{4}{3}\pi r^3\right) \\ V &= \frac{2\pi r^3}{3} \end{aligned}$$

**Ex 4.** Find the surface area and volume of each hemisphere:



$$\begin{aligned} SA &= 3\pi(10)^2 \\ &= 942.48\text{m}^2 \\ V &= \frac{2\pi(10)^3}{3} \\ &= 2094.40\text{m}^3 \end{aligned}$$



$$\begin{aligned} SA &= 3\pi(2.25)^2 \\ &= 47.71\text{yd}^2 \\ V &= \frac{2\pi(2.25)^3}{3} \\ &= 23.86\text{yd}^3 \end{aligned}$$