

Factoring - Difference of Squares

Feb 14

Review:

$$(y+2)(y-2) = y^2 - \cancel{2y} + \cancel{2y} - 4 = y^2 - 4$$

$$(x-7)(x+7) = x^2 - 49$$

$$(t-5)(t+5) = t^2 - 25$$

If given, $x^2 - 36$

Look for: 1) A difference (a minus sign)

2) Two perfect squares (can $\sqrt{\quad}$ cleanly)

$$\text{Then } \sqrt{x^2 - 36} = (x+6)(x-6)$$

$$\text{ex. } \sqrt{x^2 - 25}$$

$$(x+5)(x-5)$$

$$\text{ex. } \sqrt{\frac{x^2}{36} - \frac{16}{49}}$$

$$\left(\frac{x}{6} + \frac{4}{7}\right)\left(\frac{x}{6} - \frac{4}{7}\right)$$

$$\text{ex. } x^2 - y^2$$

$$(x-y)(x+y)$$

$$\text{ex. } 9a^2b^2 - c^2$$

$$(3ab+c)(3ab-c)$$

$$\text{ex. } \sqrt{4b^2 - 25}$$

$$(2b+5)(2b-5)$$

Trickier

$$\text{ex. } 3x^6 - 75$$

$$3(x^6 - 25)$$

$$3(x^3 + 5)(x^3 - 5)$$

$$\text{ex. } \sqrt{a^2 - \frac{1}{4}} \quad \frac{\sqrt{1}}{\sqrt{4}}$$

$$\left(a + \frac{1}{2}\right)\left(a - \frac{1}{2}\right)$$

$$\text{ex. } \sqrt{4a^2 - 16}$$

$$(2a-4)(2a+4)$$

wrong \rightarrow not fully factored

$$4(a^2 - 4)$$

$$4(a-2)(a+2)$$