## Functional Notation

## Recall:

A function can be represented by: - a graph

- a set of ordered pairs or table
- a rule or equation

Consider $y=2 x-3$
What is the value of $y$ when $x=4$ ?


How can we write this in a shorter way?


$$
\begin{aligned}
& y=2(4)-3 \\
& y=5
\end{aligned}
$$

Ex) Given $y(x)=3 x-4$, find $y(-1)$.

$$
\begin{gathered}
y(-1)=3(-1)-4 \\
y=-7
\end{gathered}
$$

The problem.. $\quad y=2 x-1$

$$
y(x)=2 x-1
$$

$$
\begin{array}{r}
y=-4 x+3 \\
y(x)=-4 x+3
\end{array}
$$

We can use other letters (f, $g$, $h$, etc.) to make the " $y$ 's" look different. $f(x)=2 x-1 \quad g(x)=-4 x+3$ ex 1) Find: a) $f\left(-\frac{\boxed{x}}{2}\right)$
b) $g(-2)$

$$
\begin{aligned}
f(-2) & =2(-2)-1 \\
& =-5
\end{aligned}
$$

ex 2) Given $f(x)=2 x-2$. Find $x$ if:
a) $\frac{f(x)}{y}=10$
$10=2 x-2$
$\frac{12}{2}=\frac{2 x}{d} \quad x=6$
b) $\frac{f(x)}{y}=-4$ $-4=2 x-12$
$\mp 2$
$-\frac{2}{2}=\frac{2 x}{2}-1=x$
ex 3) Given $g(x)=-3 x+5$. Find $x$ if:
a) $g(x)=8$
b) $g(x)=-1$
$8=-3 x+5$
-5
$-1=-3 x+5$
$\begin{aligned}-6 & =-3 x \\ x & =2\end{aligned}$

$$
-1=x
$$

ex 4) Write as an equation in two variables. (not functional notation)
a) $f(x)=3 x+1 \longrightarrow y=3 x+1$
b) $\mathrm{C}(\mathrm{n})=6-\mathrm{n} \longrightarrow \mathrm{C}=6-\mathrm{n}$
c) $t(d)=2 d \rightarrow t=2 d$
ex 5) Rewrite in functional notation.
a) $y=x+2 \longrightarrow f(x)=x+2$
b) $C=10 n-1 \rightarrow C(n)=10 n-1$
c) $t=15 d \rightarrow t(d)=15 d$

## Independent Variable

= Variable whose values are freely chosen.

## Dependent Variable

= Variable whose value depends on the independent variable
ex 6) The equation $C=25 n+100$ represents the cost, $C$, in dollars, for a feast following a sports competition, where n is the number of people attending.
a) Write the equation in function notation.

$$
C(n)=26 n+100
$$

b) State the independent and dependent variables.

$$
\text { Domain }_{x} I V=n \text {, number of people } \quad D V=C \text {, cost }{ }_{\text {Range }}
$$

c) Determine the value of $C(100)$. What does this number represent?

$$
\begin{aligned}
C(100) & =25(100)+100 \\
& =\$ 2600
\end{aligned}
$$

The cost when 100 people attend.
d) Determine the value of C 经 $=5000$. What does this number represent?

$$
\begin{aligned}
C(n) & =25 n+100 \\
5000 & =25 n+100 \\
\frac{4900}{25} & =\frac{25 n}{25} \\
n & =196 \text { people }
\end{aligned}
$$

The number of people when the cost was $\$ 5000$.

